

LETTER TO THE EDITOR

Separating the causes of orbital ordering in  
LaSr<sub>2</sub>Mn<sub>2</sub>O<sub>7</sub> using resonant soft x-ray diffraction

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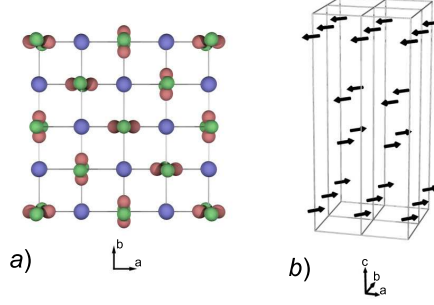
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**Abstract.** Resonant soft x-ray diffraction has been used to probe the temperature dependent orbital and magnetic structure of LaSr<sub>2</sub>Mn<sub>2</sub>O<sub>7</sub>. Previous crystallographic studies have shown that this material has almost no MnO<sub>6</sub> oxygen displacement due to Jahn-Teller distortions at low temperatures. Within the low-temperature A-type antiferromagnetic phase, we found strong intensity at the  $(\frac{1}{4}, \frac{1}{4}, 0)$  orbital and  $(0,0,1)$  magnetic reflections. This shows that even in the near absence of Jahn-Teller distortion, this compound is strongly orbitally ordered. A fit to the Mn *L*-edge resonance spectra demonstrates the presence of orbital ordering of the Mn<sup>3+</sup> ions with virtually no Jahn-Teller crystal field in addition to possible Mn<sup>3+</sup> and Mn<sup>2+</sup> like valence fluctuations.

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Ferromagnetism and charge ordering in the doped perovskite type manganese oxides R<sub>1-x</sub>A<sub>x</sub>MnO<sub>3</sub> (R = rare earth, A = Sr, Ca) have attracted considerable interest since the discovery of colossal magnetoresistance (CMR) [1]. Recently, much attention has been paid to the importance of the charge, lattice, spin and orbital degrees of freedom to explain the complex and anomalous structural, magnetic and transport behavior observed in the manganites. The interplay between these degrees of freedom can cause localisation of electrons on alternative manganese atoms to produce charge-ordered lattices. The ferromagnetism and metallic conductivity observed at low temperatures can be understood on the basis of the double-exchange mechanism whereby *e<sub>g</sub>* electrons hop between Mn sites through hybridisation with oxygen 2*p* orbitals and align the localised *t<sub>2g</sub>* spins by strong Hund's coupling [2, 3, 4]. However the understanding of the transport properties, such as CMR, and the complicated magnetic phase diagrams of the manganites requires a further ingredient, that of the orbital degree of freedom [5, 6].

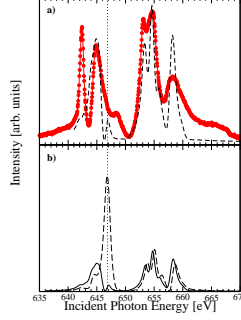


**Figure 1.** The crystal structure of the bilayer manganite  $\text{La}_{2-2x}\text{Sr}_{1+2x}\text{Mn}_2\text{O}_7$  with  $x = 0.5$  at low temperature. (a) The arrangement of the previously proposed “ $\text{Mn}^{3+}$ ” and “ $\text{Mn}^{4+}$ ” manganese ions are shown within the tetragonal unit cell. A plan view of the  $\text{Mn}^{3+}$  orbitals within the  $ab$  plane displaying orbital order of the  $x^2 - z^2, y^2 - z^2$  type is given in (a). This is the dominant type of orbital ordering found in Ref. [18] for a doping  $x = 0.42$ . Our results suggest a checkerboard pattern closer to  $\text{Mn}^{2+}/\text{Mn}^{3+}$  rather than  $\text{Mn}^{3+}/\text{Mn}^{4+}$ , however the alternating pattern remains the same. The arrangement of the magnetic spins of the  $\text{Mn}^{3+}$  ions in the low temperature antiferromagnetic structure is shown schematically in (b).

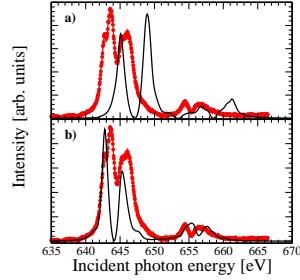
The study of the orbital ordering phenomenon is, therefore, vital for the understanding of the complex properties of the manganite systems. Direct observation of orbital ordering in manganites has recently become possible using resonant soft x-ray diffraction at the Mn  $L_{2,3}$  absorption edges after theoretical predictions by Castleton and Altarelli [7]. Mn  $L_{2,3}$  resonant x-ray scattering experiments have been performed in  $\text{La}_{0.5}\text{Sr}_{1.5}\text{MnO}_4$  [8, 9] and in  $\text{Pr}_{0.6}\text{Ca}_{0.4}\text{MnO}_3$  [10], however in both cases the orbital degree of freedom is controlled by strong Jahn-Teller distortions. In this letter we report experimental results on  $\text{LaSr}_2\text{Mn}_2\text{O}_7$ . Previous crystallographic studies [11, 12] have indicated that this system undergoes extremely small Jahn-Teller distortions at low temperature. Despite this our results demonstrate the presence of long-range orbital order, in addition to magnetic order. The fit to the orbital ordering spectrum using multiplet calculations in a crystal field shows the presence of a vanishing Jahn-Teller distortion in addition to possible  $\text{Mn}^{3+}$  and  $\text{Mn}^{2+}$  like valence fluctuations.

The samples were single crystals of the bilayer manganite  $\text{LaSr}_2\text{Mn}_2\text{O}_7$  which were melt grown in flowing oxygen using a floating zone optical image furnace. The system  $\text{La}_{2-2x}\text{Sr}_{1+2x}\text{Mn}_2\text{O}_7$  is a layered perovskite in which  $\text{MnO}_2$  double layers and  $(\text{La},\text{Sr})_2\text{O}_2$  blocking layers are stacked alternatively (see Fig 1 from Ref [12]). The reduced dimensionality causes the system to display a greatly enhanced magnetoresistance [13] and a reduced ferromagnetic transition temperature. Charge ordering has been reported in the temperature range from 100 to 200 K existing only over a narrow compositional range  $0.475 < x < 0.55$  [14, 15]. Below 170 K the  $x = 0.5$  material,  $\text{LaSr}_2\text{Mn}_2\text{O}_7$ , adopts an A-type antiferromagnetic ordering of the Mn spins [11] (see Fig. 1) and crystallographic and high-energy x-ray diffraction studies have shown the disappearance [11, 16] or reduction [17] of the Jahn-Teller distortion, such that the  $\text{MnO}_6$  octahedra are almost undistorted below  $\sim 100$  K.

Experiments were carried out using the in-vacuum diffractometer on beamline ID08 at the European Synchrotron Radiation Facility. A single crystal of  $\text{LaSr}_2\text{Mn}_2\text{O}_7$  cut with the [110] direction normal to the sample surface was used for measurements



**Figure 2.** (a) Scattered x-ray intensity as a function of incident photon energy at constant wavevector  $\mathbf{Q}_{OO} = (\frac{1}{4}, \frac{1}{4}, 0)$  (circles). The black dashed line shows the theoretical fit to the data. (b) Theoretical simulation (dashed black line) of the energy spectra with an 8-fold increase in the Jahn-Teller distortion. The fit to the experimental data is repeated for comparison (solid line).



**Figure 3.** Scattered x-ray intensity as a function of incident photon energy at a constant wavevector  $\mathbf{Q}_{AF} = (0, 0, 1)$  (red line with circles) with theoretical fits (solid black lines) describing the superposition of (a)  $\text{Mn}^{3+}/\text{Mn}^{4+}$  and (b)  $\text{Mn}^{3+}/\text{Mn}^{2+}$  type.

of the  $(\frac{1}{4}, \frac{1}{4}, 0)$  orbital order reflection. Calibration of the energy of the incident x-ray beam at ID08 by gas absorption gives an absolute accuracy of 0.2 eV at 640 eV. Measurements of the anti-ferromagnetic reflection (001), were performed on a cleaved crystal with the [001] direction surface normal. The temperature dependancies of both these reflections were obtained using beamline X1B at the National Synchrotron Light Source. At both beamlines the experimental procedure was identical to our previous studies[17, 8].

At ID08, the sample was cooled to  $\sim 20$  K using liquid helium and an intense and narrow reflection was found at a wavevector of  $\mathbf{Q}_{OO} = (\frac{1}{4}, \frac{1}{4}, 0)$  at an incident energy of 643 eV. The solid circles in Fig. 2a show the scattered intensity as a function of the incident photon energy at constant wavevector, through the manganese  $L_3$  and  $L_2$  edges. On first inspection, there appears to be two main features at the  $L_3$  edge and three at the  $L_2$  edge. In contrast to previous measurements on  $\text{La}_{0.5}\text{Sr}_{1.5}\text{MnO}_4$ [8] and  $\text{Pr}_{0.6}\text{Ca}_{0.4}\text{MnO}_3$ [10] the maximum scattered intensity is primarily observed at the  $L_2$  edge rather than at the  $L_3$  edge. Measurements of the A-type antiferromagnetic reflection in  $\text{La}_{2-2x}\text{Sr}_{1+2x}\text{Mn}_2\text{O}_7$  for  $x = 0.475$  at  $\mathbf{Q}_{AF} = (0, 0, 1)$  have been reported

by Wilkins *et al.*[17] at a temperature of 83 K. In Fig. 3(a,b) we show the scattered intensity measured at 20 K in  $\text{LaSr}_2\text{Mn}_2\text{O}_7$  as a function of energy at constant wavevector. In this case, at the  $L_2$  edge little scattering was observed but at the  $L_3$  edge very strong intensity was found which is comprised of two main features. Our experimental data in Figs. 2 and 3 indicate that  $\text{LaSr}_2\text{Mn}_2\text{O}_7$  is simultaneously orbitally and magnetically ordered at low temperature. Soft X-ray diffraction is not particularly surface-sensitive[17]. The inverse width in reciprocal space of the reflections gives an indication of the penetration depth. This indicates we are probing thousands of Ångstroms into the crystal.

In order to identify the origin of the resonant x-ray scattering signal, we have performed multiplet calculations in a crystal field. On the  $\text{Mn}^{3+}$  site with  $D_{4h}$  symmetry, two crystal field parameters are to be acquired from the fitting procedure: cubic ( $X^{400}$ ) and tetragonal ( $X^{220}$ ). In the absence of the experimental evidence, we assume that the spins are aligned in the  $[110]$  direction, which lowers the symmetry to that of the  $C_i$  point group. Choosing this direction as quantization axis, the resonant scattering amplitude at the orbital ordering wave vector  $(\frac{1}{4}, \frac{1}{4}, 0)$ , is proportional to the following combination of the atomic scattering tensors [19]:

$$f_{\text{res}}^{\text{OO}} \propto F_{0;1}^e - F_{0;-1}^e + F_{1;0}^e - F_{-1;0}^e, \quad (1)$$

with  $F_{m;m'}^e$  defined as:

$$F_{m;m'}^e = \sum_n \frac{\langle 0 | J_m^{1\dagger} | n \rangle \langle n | J_{m'}^1 | 0 \rangle}{E_0 - E_n + \hbar\omega + i\Gamma/2}, \quad (2)$$

where  $m$  and  $m'$  denote polarization states and  $J_m^1$  are the dipole operators defined in spherical coordinates.  $|0\rangle$  represents the ground state with energy  $E_0$  and  $|n\rangle$  intermediate states with energy  $E_n$ . The photon energy is  $\hbar\omega$  and  $\Gamma$  stands for the broadening due to the core-hole lifetime. Similarly, for the magnetic scattering with the wave vector  $(0,0,1)$ , the scattering amplitude can be expressed as:

$$f_{\text{res}}^{\text{MO}} \propto F_{1;1}^e - F_{-1;-1}^e. \quad (3)$$

The Slater integrals of the  $d$ - $d$  and  $p$ - $d$  direct and exchange interactions were scaled down to 75% of their atomic value. The  $p$ -shell spin-orbit parameter was increased by 9% from the Hartree-Fock value to correspond to the experimental value [20]. We used  $\Gamma = 0.5$  eV for the Lorentzian broadening due to the core-hole lifetime. In addition, to take into account also the experimental energy resolution, the scattering intensity,  $I(\hbar\omega) \propto |f_{\text{res}}|^2$ , was convoluted with a Gaussian of width 0.1 eV.

The best fit to the orbital ordering is shown in Fig. 2a. The corresponding crystal field parameters are  $X^{400} = 3$  eV and  $X^{220} = 0.4$  eV, (or  $10D_q = 0.91$  eV and  $D_s = -0.048$  eV). The fit did not significantly change for variations of the cubic field  $X^{400}$  in the interval 3–4 eV and for the tetragonal (Jahn-Teller) field  $X^{220}$  in the interval 0.1–0.6 eV. The fit displays a fair general agreement with the experimental spectrum. The obtained  $L_3/L_2$  ratio is satisfactory and we reproduce most of the structure from the experimental spectrum. However, the first peak in the  $L_3$  edge is not reproduced [21] and broadened high-energy features at both edges are missing in the fit. These wide shoulders may be related to band-structure effects, which are not incorporated in our model. In Fig. 2b we illustrate the effect of an 8-fold increase of the Jahn-Teller field. As shown before, [22], the  $L_3/L_2$  ratio is becoming larger with the increase in the tetragonal component of the crystal field. In our calculations a small Jahn-Teller tetragonal crystal field is necessary to lift the degeneracy of the  $e_g$

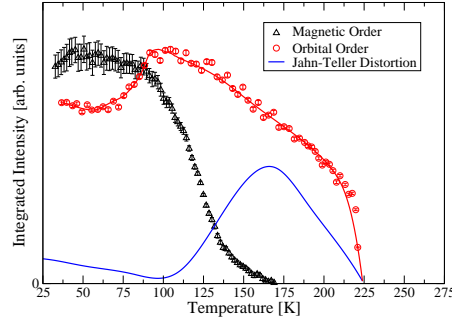
levels, however the tetragonal field included is extremely small. Its value is one order of magnitude smaller than that obtained, *e.g.*, for  $\text{La}_{0.5}\text{Sr}_{1.5}\text{MnO}_4$  [22], so that, except for the lifting of orbital degeneracy, the  $\text{Mn}^{3+}$  ion is essentially in a cubic field. This shows we are within a regime where the scattering is dominated by orbital ordering of the  $e_g$  electrons.

We were not able to obtain a good fit to the magnetic scattering with  $\text{Mn}^{3+}$  ions alone, as it gave a single peak at each edge. Since the  $\mathbf{Q}_{AF} = (0, 0, 1)$  sees a superposition of *all* manganese ions within the  $ab$  plane, we included an additional type of Mn ion in our model. Figure 3a shows the magnetic spectrum obtained by superposing the contributions of  $\text{Mn}^{3+}$  and  $\text{Mn}^{4+}$  with equal weights. The  $\text{Mn}^{4+}$  ion induces a peak at higher energy (at both edges) relative to the  $\text{Mn}^{3+}$  ion, as expected for ions with larger oxidation number[23]. This gives rise to a spectrum with two peaks at each edge, but shifted to a higher energy relative to the experimental spectrum. Moreover, the ratio between the two main features at both the  $L_3$  and  $L_2$  edges is inverted. In order to reproduce the feature at low energy, with a ratio consistent with experiment, we need to consider a Mn ion with lower oxidation number. In panel b) of Fig. 3 we show the spectrum obtained with a 1:1 ratio of  $\text{Mn}^{2+}$  and  $\text{Mn}^{3+}$ . In these calculations, the  $\text{Mn}^{3+}$  crystal field parameters were taken to be exactly the same as for the orbital spectrum in Fig. 2a, and the  $\text{Mn}^{2+}$  and  $\text{Mn}^{4+}$  spectra were calculated in a purely cubic crystal field ( $X^{400} = 3.0$  eV). In Fig. 3, we positioned the  $\text{Mn}^{2+}$  ( $\text{Mn}^{4+}$ ) edge, relative to the  $\text{Mn}^{3+}$  edge, using the theoretical chemical shifts obtained from our atomic multiplet calculations, *i.e.*  $\sim -2$  eV and 4 eV, respectively. Experimental L-edge absorption results on  $\text{Mn}^{2+}$ ,  $\text{Mn}^{3+}$ , and  $\text{Mn}^{4+}$  reference compounds show comparable chemical shifts (between -1 and -2 eV for  $\text{Mn}^{2+}$  and between 2 and 3 eV for  $\text{Mn}^{4+}$  [24, 25, 26]).

Surprisingly, much better agreement with the experimental data in Fig. 3(a,b) is obtained by the calculation for the  $\text{Mn}^{2+}/\text{Mn}^{3+}$  case than for the  $\text{Mn}^{3+}/\text{Mn}^{4+}$  case. This may simply reflect the basic limitations of the atomic multiplet calculations (which, for one thing, only allow integer values for the valence) to describe an extended system with non-negligible interatomic hopping; on the other hand, it is noteworthy that an average valence between 2+ and 3+ has recently been suggested by Hartree-Fock calculations [27, 28], and experimental data which indicate that the additional holes reside more on the oxygen ligands [29, 30]. Such a change in the manganese valency from 3+/4+ to 2+/3+ would not alter the orbital occupancy of the  $\text{Mn}^{3+}$  ion. Both  $\text{Mn}^{2+}$  and  $\text{Mn}^{4+}$  are not Jahn-Teller active.

Figure 4 shows the temperature dependence of the orbital and magnetic reflections. The  $(\frac{1}{4}, \frac{1}{4}, 0)$  reflection is observed below  $T_{OO}$  which is coincident with  $T_{JT}$ . The Jahn-Teller distortions maximise at  $T_N$  ( $\sim 170$  K) and decrease below this temperature due to the occurrence of antiferromagnetic interactions. Note that the Jahn-Teller distortions are very weak below 100 K where the orbital and magnetic reflections are very strong. We note that below 100 K the Jahn-Teller distortions increase slightly, which coincides with a change in gradient of the intensity of the orbital and magnetic reflections.

In conclusion, we have reported the results of resonant soft x-ray scattering studies of the orbital and antiferromagnetic ordering in  $\text{LaSr}_2\text{Mn}_2\text{O}_7$ . The data of Fig. 2 and 3 immediately show that  $\text{LaSr}_2\text{Mn}_2\text{O}_7$  is simultaneously both orbitally and antiferromagnetically ordered at low temperatures, despite the fact that the Jahn-Teller distortions in this system are measured to be very small. This is further supported by the theoretical fits, which display a good agreement with the



**Figure 4.** Temperature dependence of the integrated intensity of the  $(\frac{1}{4}, \frac{1}{4}, 0)$  orbital order reflection and the  $(001)$  magnetic order reflection. The temperature dependence of the  $(\frac{3}{4}, -\frac{1}{4}, 5)$  Jahn-Teller distortion peak, a measure of the amplitude of the Jahn-Teller distortion, is taken from Ref [12].

experimental data for very small values of tetragonal crystal field. From these we can conclude that it is possible to obtain a strongly orbitally ordered phase within an A-type antiferromagnetic configuration in the absence of significant Jahn-Teller distortions. In such case, the energetics of the orbitally ordered configuration is favored by the magnetic interactions, originating from the superexchange mechanism, as described by Goodenough, [31]. The fit to the magnetic scattering data suggests a fluctuating valence situation, with Mn ions with valence charge between +3 and +2.

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